

# *An Interleaved Dual-Battery Power Supply for Battery-Operated Electronics*

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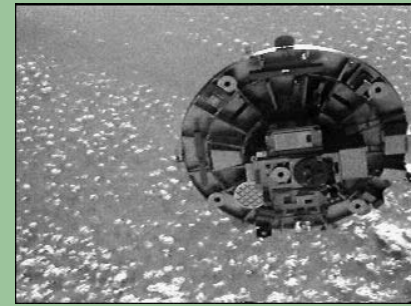
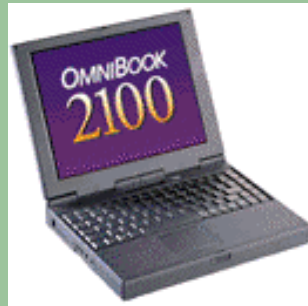
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# *Outline*

- ❖ **Introduction**
- ❖ **Background**
- ❖ **Analysis of Optimal Supply Voltage**
- ❖ **Design of Interleaved Dual-Battery Power Supply**
- ❖ **Conclusions**

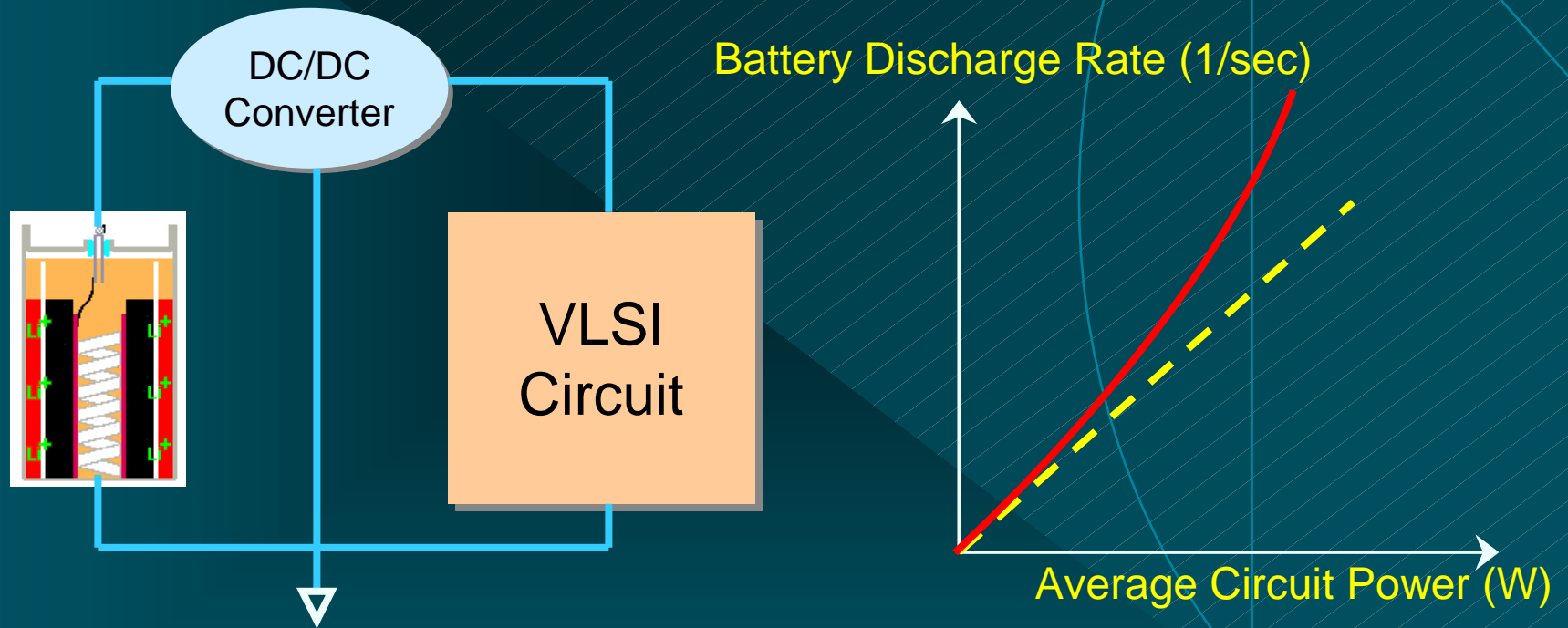
# Batteries in Mobile/Portable Electronics

Extending the battery service life for mobile electronics is a major motivation for low power design



# Battery Power Supply System

In reality, the battery discharge rate is **super-linearly** related to the average power consumption in the VLSI circuit



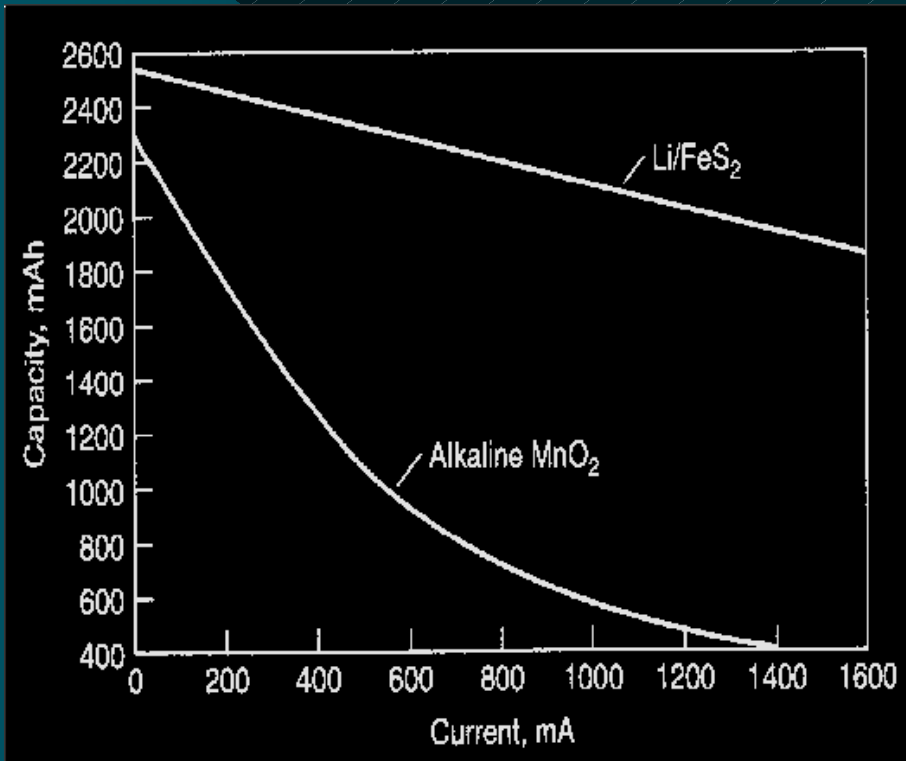
# ***Low Power Design Metrics***

- ❖ **Energy-delay (E-D) product [M. Horowitz, et al, 1994]**
  - ◆ Measures circuit speed for energy dissipation per operation
  - ◆ Does not consider the characteristics of the battery power supply system
- ❖ **Battery discharge-delay (BD-D) product [M. Pedram, et al, 1999]**
  - ◆ Measures circuit speed for battery discharge per operation
  - ◆ Only considers the current-capacity characteristics of the battery

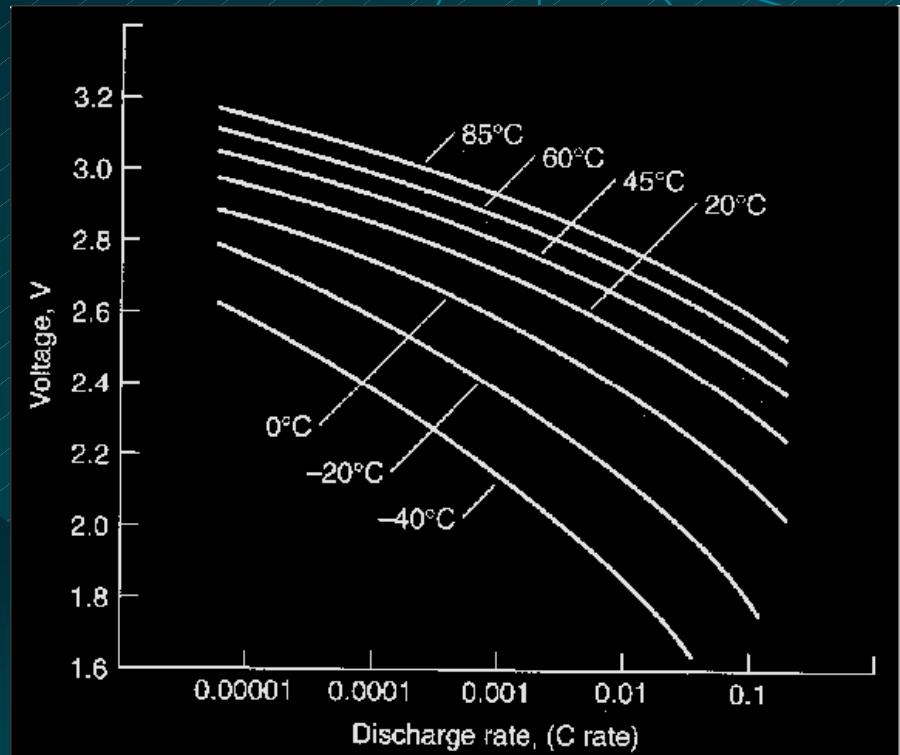
# ***In This Paper***

- ❖ **Further analysis of the BD-D product**
  - ◆ **Considers the current-voltage characteristics of the battery, in addition to its current-capacity characteristics**
- ❖ **Design of an Interleaved Dual-Battery (IDB) power supply system**
  - ◆ **Uses two batteries of different current-capacity characteristics**
  - ◆ **Calculates the optimal combination of the two battery types**
  - ◆ **Increases the battery life time**

# Battery Characteristics



**Current-capacity**



**Current-voltage**

# ***An Analytical Model***

**Actual battery energy discharge**

$$E^{act} = \frac{V_0 \cdot I_0 \cdot T}{\mu}, \quad 0 \leq \mu \leq 1$$

**Efficiency factor (current-capacity relation)**

$$\mu = 1 - \beta \cdot I_0$$

**Output voltage function (current-voltage relation)**

$$V_0 = V^{OC} - \gamma \cdot I_0$$

**Conversion efficiency equation (DC/DC converter)**

$$\eta \cdot V_0 \cdot I_0 = V_{dd} \cdot I_{dd}$$



# Battery Discharge (BD)

## Definition

$$BD = \frac{E^{act}}{CAP_0} = \frac{V_0(I_0) \cdot I_0 \cdot T}{CAP_0 \cdot \mu(I_0)}$$

## Energy dissipation of the VLSI circuit

$$V_{dd} \cdot I_{dd} \cdot T = \frac{1}{2} C_{sw} \cdot V_{dd}^2$$

## BD as a function of $V_{dd}$ and $I_0$

$$BD = \frac{C_{sw}}{2 \cdot \eta \cdot CAP_0} \cdot \frac{V_{dd}^2}{1 - \beta \cdot I_0}$$

# Calculating the Battery Discharge Current

Relation between  $V_{dd}$  and  $I_0$

$$\eta \cdot (V^{OC} - \gamma \cdot I_0) \cdot I_0 \cdot T = \frac{1}{2} C_{sw} \cdot V_{dd}^2$$

$I_0$  as a function of  $V_{dd}$

$$I_0 = \frac{\eta \cdot V^{OC} - \sqrt{\eta^2 \cdot (V^{OC})^2 - 2 \cdot \eta \cdot \gamma \cdot C_{sw} \cdot V_{dd}^2} / T}{2 \cdot \eta \cdot \gamma}$$

# ***BD-Delay (BD-D) Product***

**Delay of CMOS circuits**

$$t_d = m \frac{V_{dd}}{(V_{dd} - V_{th})^\alpha}, \quad 1 < \alpha \leq 2$$

**BD-D product**

$$BD-D = \frac{m \cdot C_{sw}}{2 \cdot \eta \cdot CAP_0} \cdot \frac{V_{dd}^3}{(1 - \beta \cdot I_0) \cdot (V_{dd} - V_{th})^\alpha}$$

# Determining the Cycle Time

Assuming clock cycle time is proportional to circuit delay

$$T \propto t_d \Rightarrow T = m' \frac{V_{dd}}{(V_{dd} - V_{th})^\alpha}, \quad 1 < \alpha \leq 2$$

Complete expression for battery discharge current

$$I_0 = \frac{\eta \cdot V^{OC} - \sqrt{\eta^2 \cdot (V^{OC})^2 - 2 \cdot \eta \cdot \gamma \cdot C_{sw} \cdot V_{dd} \cdot (V_{dd} - V_{th})^\alpha} / m'}{2 \cdot \eta \cdot \gamma}$$

By substituting  $I_0$  in the expression for BD-D , we can obtain a complicated expression for BD-D in which  $V_{dd}$  is the only variable.

# An Example

Assume a VLSI circuit consumes 13.5W power at supply voltage of 1.5V

Parameter	Value	Comment
$V_0$	4V	Typical lithium battery
$\eta$	0.9	Typical DC/DC converter
$C_{sw}/m'$	21	Calculated
$\alpha$	1.5	Typical CMOS technology
$V_{th}$	0.6	Typical CMOS technology
$\frac{m \cdot C_{sw}}{2 \cdot \eta \cdot CAP_0}$	1	Normalized

$$\beta = \{0, 0.05, 0.1, 0.15\} \quad \gamma = \{0, 0.15, 0.3\}$$

# BD-D Curves

*BD-D* product



$$\beta=0.15, \gamma=0.3$$

$$\beta=0.1, \gamma=0.3$$

$$\beta=0.1, \gamma=0.15$$

$$\beta=0.1, \gamma=0$$

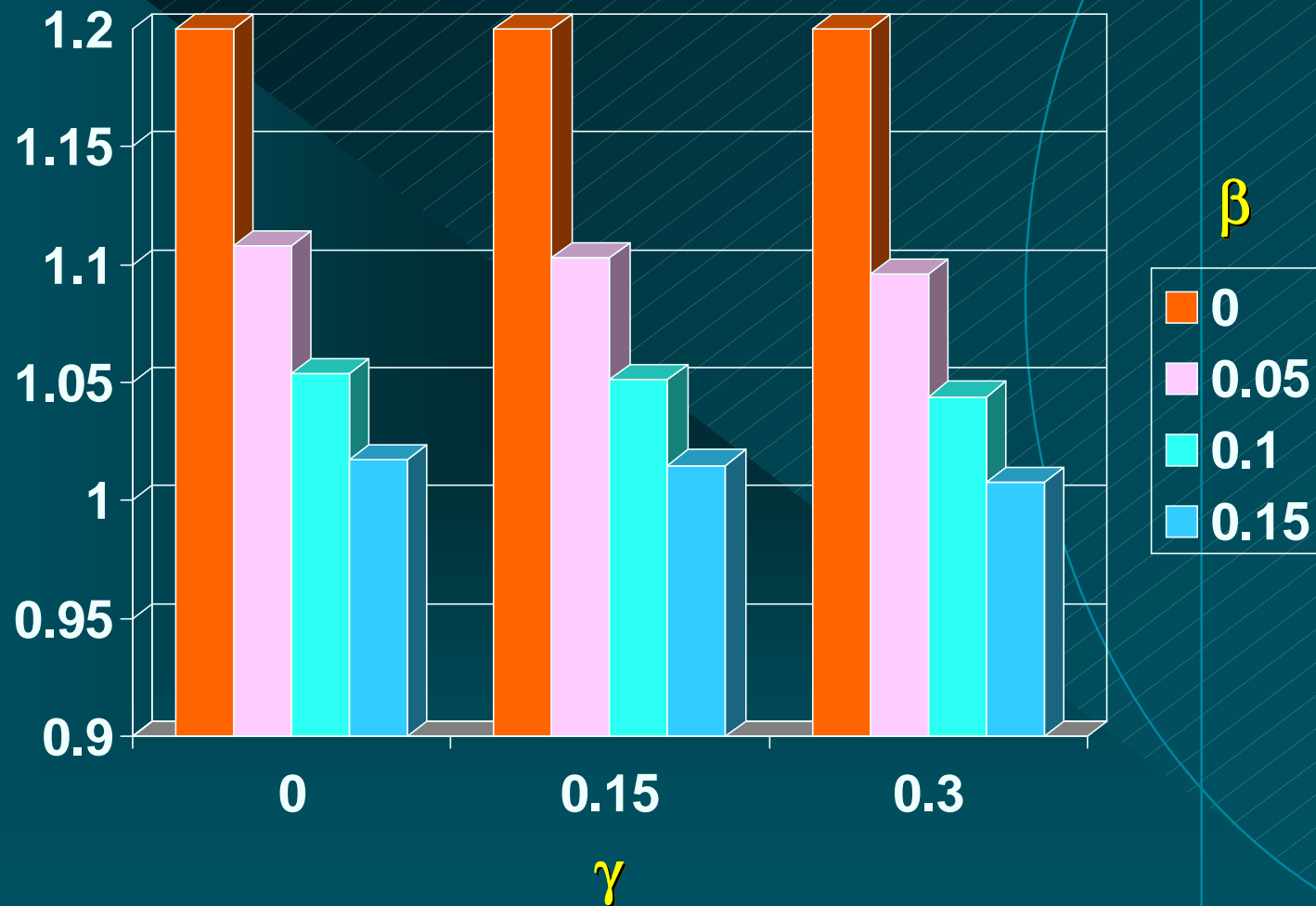
$$\beta=0.05, \gamma=0.3$$

$$\beta=0, \gamma=0 \text{ (ideal case)}$$

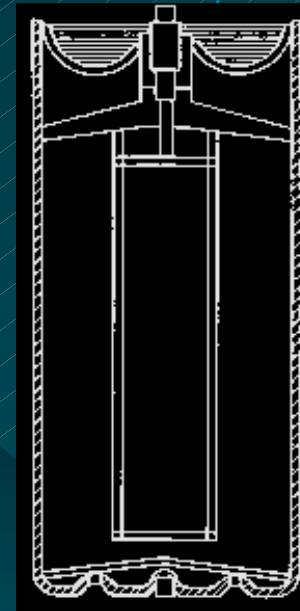
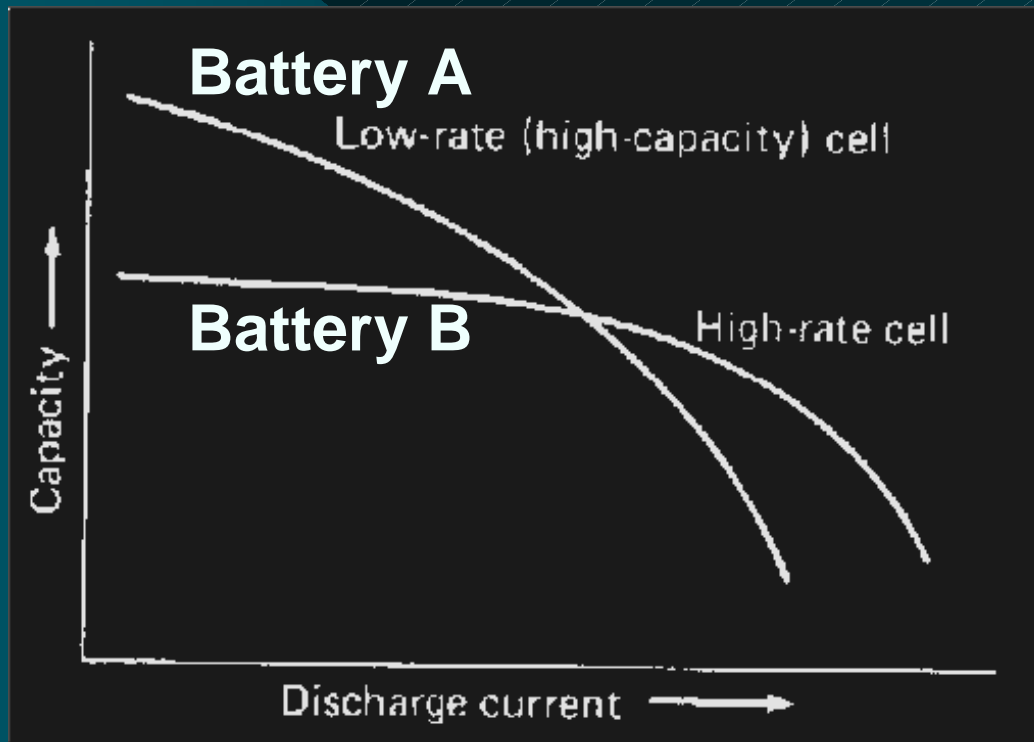
$V_{dd}(\text{V})$

# Optimal $V_{dd}$ Values

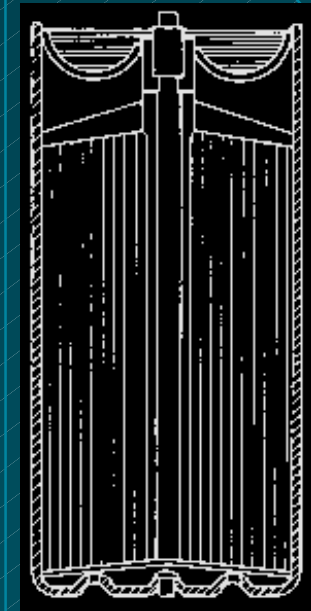
Optimal  $V_{dd}$  (V)



# Batteries with Different Characteristics



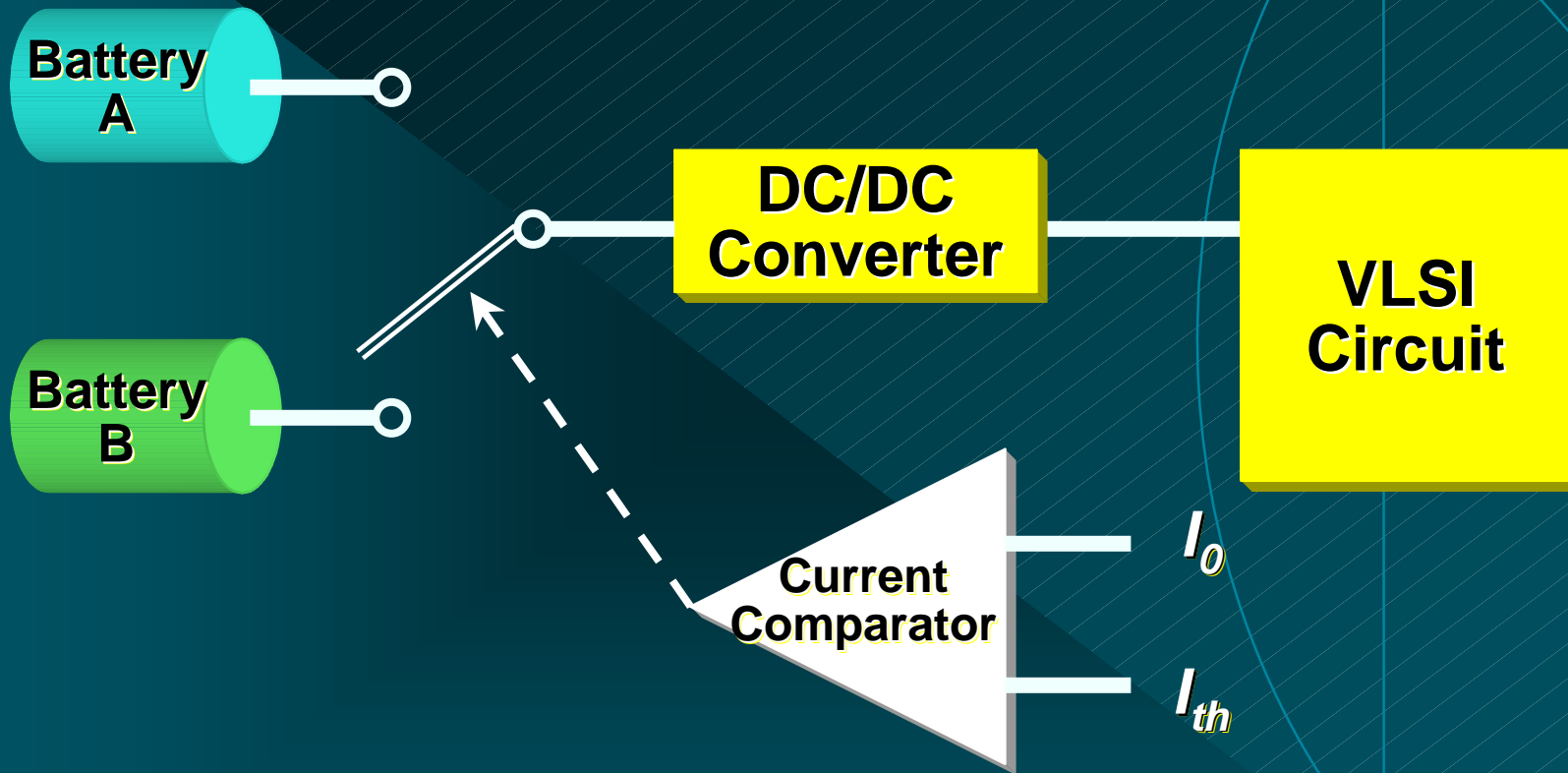
bobbin cell



spiral cell



# Block Diagram for the IDB Power Supply System

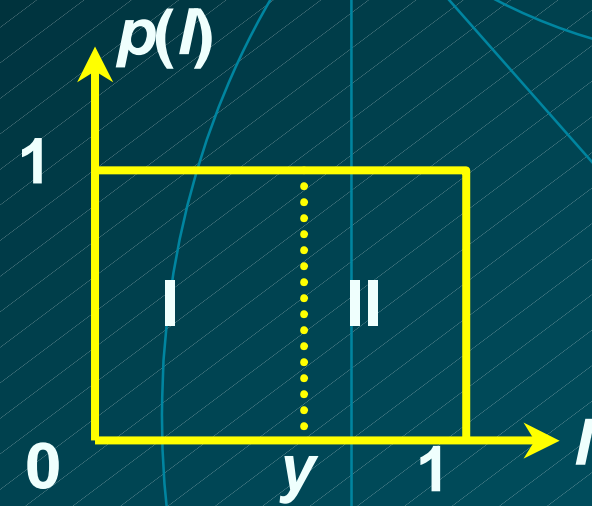
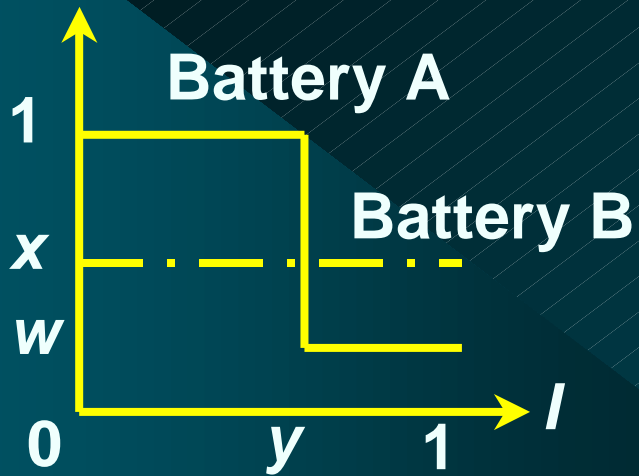


# ***Design Problem Statement***

- ❖ **Given:**
  - ◆ **Two batteries with different current-capacity characteristics**
  - ◆ **Current dissipation profile of the VLSI circuit**
  - ◆ **A volume (or weight) limit (normalized to 1) for the power supply**
- ❖ **Divide the total battery volume (or weight) between these two battery types such that the service life of the IDB power supply system is maximized**

# Analysis Setup

Capacity (Battery efficiency  $\mu$ )



Battery Service Life (BSL)

$$BSL = 1 / I_{ave}^{act}$$

# *Single Battery Power Supply*

Using Battery A only

$$BSL = 2w / (1 - (1 - w)y^2)$$

Using Battery B only

$$BSL = 2x$$

# IDB Power Supply

Optimal threshold current

$$I_{th} = y \Rightarrow \begin{cases} \text{use Battery A} & \text{if } I_0 < y \\ \text{use Battery B} & \text{if } I_0 \geq y \end{cases}$$

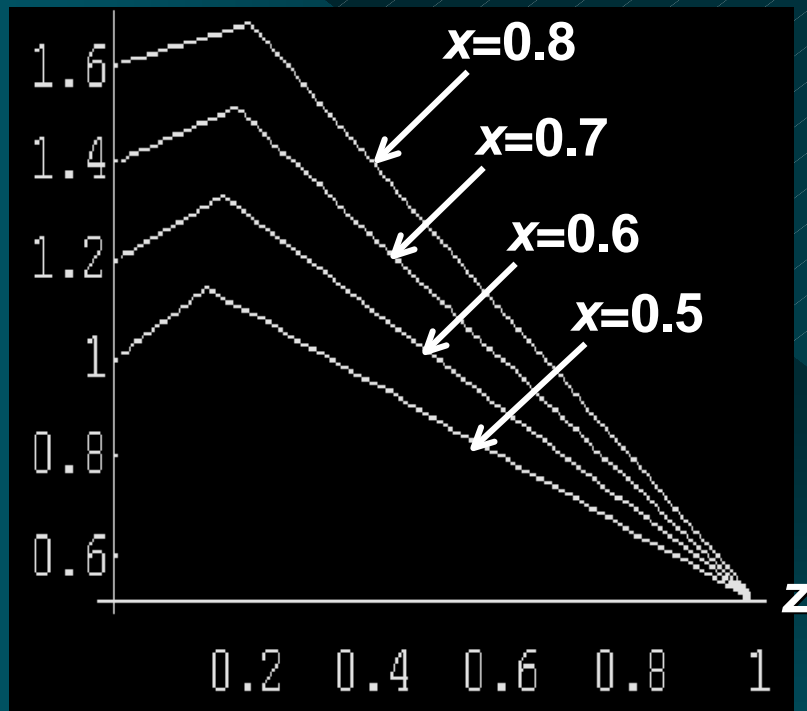
Optimal weight/volume distribution of the power supply

$$z^* = (xy^2) / (1 - y^2 + xy^2), \quad 0 \leq z^* \leq 1$$

⇒ Battery A occupies a portion of  $z^*$   
Battery B occupies a portion of  $(1-z^*)$

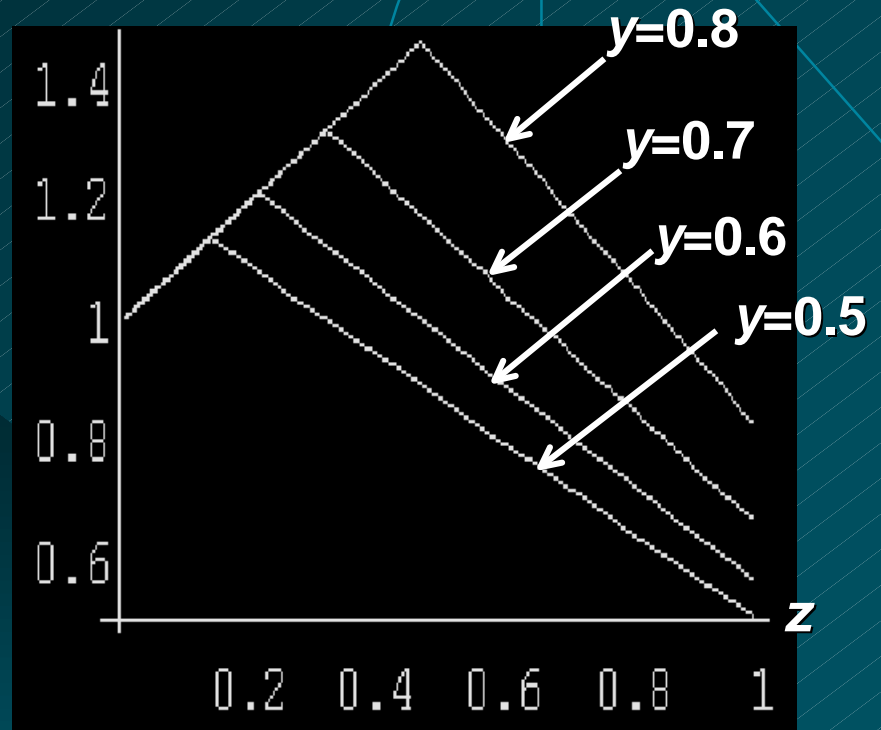
# ***BSL as a Function of $x$ , $y$ and $z$***

***BSL***



**(a)  $y$  is fixed at 0.5**

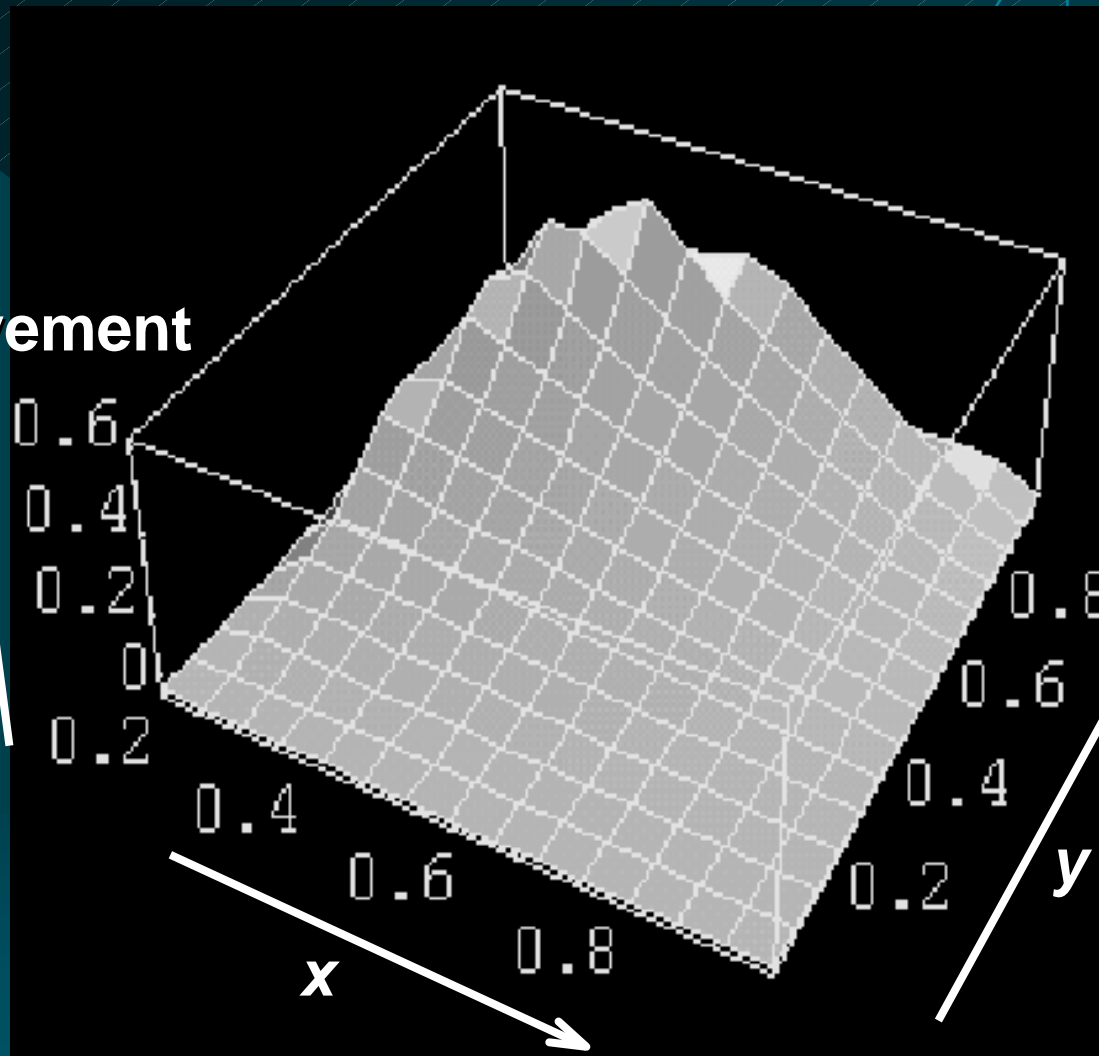
***BSL***



**(b)  $x$  is fixed at 0.5**

# ***BSL Improvement Plot***

***BSL improvement***



# ***Conclusions***

- ❖ **It is important to consider the current-voltage characteristic of the battery in addition to its current-capacity characteristic.**
- ❖ **By appropriately combining batteries with different current-capacity characteristics (w.r.t. optimal portion of each battery type), the IDB power supply can significantly extend the battery service life.**